

Gaps & Intervals — Practice

CKSTEM Math Problem Solving · Grades 4–7

- 1** IF N OBJECTS SIT IN A LINE WITH ONE AT EACH END, THEN THERE ARE $N - 1$ SPACES BETWEEN THEM — ALWAYS ONE LESS.

Seven fence posts stand in a straight line along a yard, with a post at each end. How many spaces sit between neighbouring posts?

WORK IT OUT HERE

- 2** IF N OBJECTS SIT IN A LINE WITH ONE AT EACH END, THEN THERE ARE $N - 1$ SPACES BETWEEN THEM — ALWAYS ONE LESS.

A long ribbon has 12 knots tied along it, with a knot at each end. How many sections of ribbon sit between neighbouring knots?

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- 3** IF N OBJECTS SIT IN A LINE WITH ONE AT EACH END, THEN THERE ARE $N - 1$ SPACES BETWEEN THEM — ALWAYS ONE LESS.

A garland is strung from one wall to the other with 25 small lights along it, one light touching each wall. How many gaps separate neighbouring lights?

WORK IT OUT HERE

- 4** IF N OBJECTS ARE EQUALLY SPACED FROM END TO END, THEN $\text{GAP} = \text{TOTAL} \div (N - 1)$ —
DIVIDE BY SPACES, NOT BY OBJECTS.

A caretaker sets up 5 lamp posts along a 24 m garden walkway, with a lamp at each end and the same distance between neighbours. How far apart are neighbouring lamps?

WORK IT OUT HERE

- 5** IF N OBJECTS ARE EQUALLY SPACED FROM END TO END, THEN $\text{GAP} = \text{TOTAL} \div (N - 1)$ —
DIVIDE BY SPACES, NOT BY OBJECTS.

A coach plants 11 flags equally spaced along an 80 m sideline, with a flag at each end. What is the distance between neighbouring flags?

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- 6** IF N OBJECTS ARE EQUALLY SPACED FROM END TO END, THEN $\text{GAP} = \text{TOTAL} \div (N - 1)$ —
DIVIDE BY SPACES, NOT BY OBJECTS.

A swim official places 13 buoys equally spaced across a 144 m lake, with a buoy at each shore. What is the distance between neighbouring buoys?

WORK IT OUT HERE

7 IF EQUALLY-SPACED OBJECTS ARE NUMBERED 1..N, THEN THE DISTANCE FROM OBJECT I TO OBJECT J IS $|J - I| \times \text{GAP}$ — COUNT THE GAPS YOU CROSS, NOT THE STOPS.

Eight chairs sit in a straight line 3 m apart, with a chair at each end. How far is it from chair 2 to chair 5?

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8 IF EQUALLY-SPACED OBJECTS ARE NUMBERED 1..N, THEN THE DISTANCE FROM OBJECT I TO OBJECT J IS $|J - I| \times \text{GAP}$ — COUNT THE GAPS YOU CROSS, NOT THE STOPS.

Twelve hydro poles stand equally spaced in a straight line, with neighbouring poles 25 m apart. How far is it from the 4th pole to the 11th pole?

WORK IT OUT HERE

9 IF EQUALLY-SPACED OBJECTS ARE NUMBERED 1..N, THEN THE DISTANCE FROM OBJECT I TO OBJECT J IS $|J - I| \times \text{GAP}$ — COUNT THE GAPS YOU CROSS, NOT THE STOPS.

Twenty-one banners hang equally spaced along a 160 m parade route, with a banner at each end. How far is it from banner 4 to banner 17?

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- 10** IF DEPARTURES (OR STRIKES / EVENTS) ARE AT EQUAL TIME INTERVALS WITH BOTH ENDPOINTS KNOWN, THEN $(\text{LAST} - \text{FIRST}) \div (N - 1) = \text{INTERVAL}$. TIMES ARE POINTS ON A LINE.

A school rings 6 bells at equal time intervals during the morning. The first bell rings at 7:00 a.m. and the last rings at 7:30 a.m. How many minutes pass between neighbouring bells?

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- 11** IF DEPARTURES (OR STRIKES / EVENTS) ARE AT EQUAL TIME INTERVALS WITH BOTH ENDPOINTS KNOWN, THEN $(\text{LAST} - \text{FIRST}) \div (N - 1) = \text{INTERVAL}$. TIMES ARE POINTS ON A LINE.

Trains leave a station at equal time intervals. The first train leaves at 6:00 a.m. and the last leaves at 9:00 a.m., with 13 trains in total. How many minutes pass between neighbouring trains?

WORK IT OUT HERE

- 12** IF DEPARTURES (OR STRIKES / EVENTS) ARE AT EQUAL TIME INTERVALS WITH BOTH ENDPOINTS KNOWN, THEN $(\text{LAST} - \text{FIRST}) \div (N - 1) = \text{INTERVAL}$. TIMES ARE POINTS ON A LINE.

A fountain runs equally spaced shows from 11:10 a.m. to 4:10 p.m. on the same day, with 11 shows in total. How many minutes apart are neighbouring shows?

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13 IF A REGULAR PATTERN WOULD PLACE N_0 OBJECTS BUT SOME POSITIONS ARE BLOCKED (END CLEARANCES, EXCLUDED ZONES), THEN COUNT = $N_0 - (\text{BLOCKED})$; SUBTRACT, NEVER RECOUNT.

A 40 m railing has a post every 4 m, with a post position at each end. For accessibility, all posts within 4 m of either end are removed. How many posts remain?

WORK IT OUT HERE

14 IF A REGULAR PATTERN WOULD PLACE N_0 OBJECTS BUT SOME POSITIONS ARE BLOCKED (END CLEARANCES, EXCLUDED ZONES), THEN COUNT = $N_0 - (\text{BLOCKED})$; SUBTRACT, NEVER RECOUNT.

A 90 m walkway is lined with bollards every 6 m, with a bollard position at each end. No bollards may sit between 30 m and 48 m (driveway), endpoints included. How many bollards are placed?

WORK IT OUT HERE

15 IF A REGULAR PATTERN WOULD PLACE N_0 OBJECTS BUT SOME POSITIONS ARE BLOCKED (END CLEARANCES, EXCLUDED ZONES), THEN COUNT = $N_0 - (\text{BLOCKED})$; SUBTRACT, NEVER RECOUNT.

A 200 m hiking trail has a distance marker every 10 m, with a marker position at each end. Two restrictions apply: no markers at any position within 20 m of either end, endpoints included; and no markers from 90 m to 120 m, endpoints included. How many markers are placed?

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- 16** IF TWO PLANS (DIFFERENT SPACING, DIFFERENT COUNT) BOTH FIT THE SAME FIXED CORRIDOR, THEN $(N_1 - 1) \times G_1 = (N_2 - 1) \times G_2$ — EQUATE SPACES \times GAP.

Two plans line the SAME hallway, each with an object at each end. Plan A places 5 chairs spaced 6 m apart. Plan B places 4 chairs equally spaced along the same hallway. What is the spacing in Plan B?

WORK IT OUT HERE

- 17** IF TWO PLANS (DIFFERENT SPACING, DIFFERENT COUNT) BOTH FIT THE SAME FIXED CORRIDOR, THEN $(N_1 - 1) \times G_1 = (N_2 - 1) \times G_2$ — EQUATE SPACES \times GAP.

Two planting plans cover the SAME path, each with a tree at each end. Plan A uses 11 trees spaced x m apart. Plan B uses 6 trees spaced $(x + 5)$ m apart. Find x .

WORK IT OUT HERE

- 18** IF TWO PLANS (DIFFERENT SPACING, DIFFERENT COUNT) BOTH FIT THE SAME FIXED CORRIDOR, THEN $(N_1 - 1) \times G_1 = (N_2 - 1) \times G_2$ — EQUATE SPACES \times GAP.

Two seating plans line the SAME corridor, each with a chair at each end. Plan A uses 13 chairs spaced x m apart. Plan B uses 9 chairs spaced $(x + 2)$ m apart. Find x and the corridor length.

WORK IT OUT HERE

Answer Key

Each answer comes with a hint that names the move. The tag says which video to rewatch if you are stuck.

1. 6 spaces — *If N objects sit in a line with one at each end, then there are $N - 1$ spaces between them — always one less.*

Use Posts and Spaces — line them up with one at each end, then count one fewer than the number of posts.

2. 11 sections — *If N objects sit in a line with one at each end, then there are $N - 1$ spaces between them — always one less.*

Treat the knots as posts in a line — the sections are the spaces between them.

3. 24 gaps — *If N objects sit in a line with one at each end, then there are $N - 1$ spaces between them — always one less.*

Lights at both walls means lights at both ends — apply Posts and Spaces to count the gaps.

4. 6 m — *If N objects are equally spaced from end to end, then $gap = total \div (N - 1)$ — divide by spaces, not by objects.*

Use Count the Spaces — first figure out how many gaps the lamps make between them, then use that count with the total length.

5. 8 m — *If N objects are equally spaced from end to end, then $gap = total \div (N - 1)$ — divide by spaces, not by objects.*

First count how many gaps the 11 flags create, then divide the 80 m total by that number of gaps.

6. 12 m — *If N objects are equally spaced from end to end, then $gap = total \div (N - 1)$ — divide by spaces, not by objects.*

Use Count the Spaces — find the number of gaps the buoys make first, then divide the lake width by that.

7. 9 m — *If equally-spaced objects are numbered $1..N$, then the distance from object i to object j is $|j - i| \times gap$ — count the gaps you cross, not the stops.*

Count the gaps between chair 2 and chair 5, then multiply by the spacing — do not count the chairs themselves.

8. 175 m — *If equally-spaced objects are numbered $1..N$, then the distance from object i to object j is $|j - i| \times gap$ — count the gaps you cross, not the stops.*

The number of 25 m gaps between the 4th and 11th pole is the difference of their position numbers — multiply that count by the spacing.

9. 104 m — *If equally-spaced objects are numbered $1..N$, then the distance from object i to object j is $|j - i| \times gap$ — count the gaps you cross, not the stops.*

Use Position to Position — but the spacing is not given directly, so figure out the size of one gap from the total route first.

10. 6 minutes — *If departures (or strikes / events) are at equal time intervals with both endpoints known, then $(last - first) \div (N - 1) = interval$. Times are points on a line.*

Treat the bell times as posts on a timeline — find the number of gaps between the 6 bells, then divide the 30-minute span by that count.

11. 15 minutes — *If departures (or strikes / events) are at equal time intervals with both endpoints known, then $(last - first) \div (N - 1) = interval$. Times are points on a line.*

Convert the span from 6:00 to 9:00 into minutes, then divide by the number of gaps the 13 trains create on the timeline.

12. 30 minutes — *If departures (or strikes / events) are at equal time intervals with both endpoints known, then $(\text{last} - \text{first}) \div (N - 1) = \text{interval}$. Times are points on a line.*

First convert the time span from 11:10 a.m. to 4:10 p.m. into minutes, then divide by the count of gaps that the 11 shows make on the timeline.

13. 7 posts — *If a regular pattern would place N_o objects but some positions are blocked (end clearances, excluded zones), then $\text{count} = N_o - (\text{blocked})$; subtract, never recount.*

Use Pattern Minus Forbidden — count every position from 0 m to 40 m as if no rule applied, then subtract the ones inside the end-clearance zones.

14. 12 bollards — *If a regular pattern would place N_o objects but some positions are blocked (end clearances, excluded zones), then $\text{count} = N_o - (\text{blocked})$; subtract, never recount.*

Count the full unrestricted pattern of bollard positions first, then subtract the positions that fall inside the driveway zone.

15. 11 markers — *If a regular pattern would place N_o objects but some positions are blocked (end clearances, excluded zones), then $\text{count} = N_o - (\text{blocked})$; subtract, never recount.*

Use Pattern Minus Forbidden — list every marker position from 0 m to 200 m as if no rule applied, then subtract the positions blocked by the end clearances and the positions blocked by the mid-trail zone.

16. 8 m — *If two plans (different spacing, different count) both fit the same fixed corridor, then $(N_1 - 1) \times g_1 = (N_2 - 1) \times g_2$ — equate spaces \times gap.*

Write Plan A's hallway length as spaces times gap, then set Plan B's spaces times its unknown gap equal to that same length.

17. 5 m (with path length 50 m) — *If two plans (different spacing, different count) both fit the same fixed corridor, then $(N_1 - 1) \times g_1 = (N_2 - 1) \times g_2$ — equate spaces \times gap.*

Write the path length two ways — Plan A as 10 gaps of x , Plan B as 5 gaps of $(x + 5)$ — set them equal and solve for x .

18. 4 m (with corridor length 48 m) — *If two plans (different spacing, different count) both fit the same fixed corridor, then $(N_1 - 1) \times g_1 = (N_2 - 1) \times g_2$ — equate spaces \times gap.*

Write the corridor length two ways using each plan's spaces times its gap, set the two expressions equal, and solve for x .